

Name _____

Date _____

Unit 3 · Place value and rounding — teaching slides

12 slides, formatted for printing.

3.1 Multiplying and dividing by powers of 10

Powers of 10

- A power of 10 is 10 multiplied by itself a number of times.
- The small raised number is the **index**.
- The index also tells you how many zeros the number has.

$$\begin{aligned}10^1 &= 10 \\10^2 &= 100 \\10^3 &= 1000 \\10^6 &= 1\,000\,000\end{aligned}$$

Multiplying by a power of 10

- Multiplying makes a number **bigger**.
- Every digit moves to the **left**.
- The number of places is the index.
- Fill any gaps with zeros.

$$\begin{aligned}3.7 \times 10^3 &\rightarrow \text{digits move 3 left} \rightarrow 3700 \\0.39 \times 10^5 &\rightarrow \text{digits move 5 left} \rightarrow 39\,000\end{aligned}$$

Dividing by a power of 10

- Dividing makes a number **smaller**.
- Every digit moves to the **right**.
- Again, the number of places is the index.

$$\begin{aligned}80\,000 \div 10^4 &\rightarrow \text{digits move 4 right} \rightarrow 8 \\45.6 \div 10^2 &\rightarrow \text{digits move 2 right} \rightarrow 0.456\end{aligned}$$

Careful with 'crossing off zeros'

- Some people delete zeros instead of moving the digits.
- That works only when the number ends in enough zeros.
- Moving the digits always works.

$80\ 000 \div 10^4 = 8$ ✓ four zeros to remove
 $45 \div 10^4 = 0.0045$ × no zeros to remove
 $2\ 350\ 000 \div 10^5 = 23.5$ × only four zeros, index is 5

Working backwards

- Multiplying and dividing by 10^n are inverse operations.
- If you know the answer, undo the move to find the start.

$? \times 10^3 = 4500 \rightarrow 4500 \div 10^3 = 4.5$
 $? \div 10^4 = 0.007 \rightarrow 0.007 \times 10^4 = 70$

Why this matters

- Every metric conversion is a power of 10.
- So is every change between millions, thousands and units.
- Get this right and unit conversion becomes automatic.

$25\ \text{kg} = 25 \times 10^3\ \text{g} = 25\ 000\ \text{g}$
 $8460\ \text{m} = 8460 \div 10^3\ \text{km} = 8.46\ \text{km}$
 $7.2\ \text{m} = 7.2 \times 10^2\ \text{cm} = 720\ \text{cm}$

3.2 Rounding

Why round at all?

- Measurements and divisions often give more digits than anyone needs.
- The **degree of accuracy** says how precise the answer should be.
- Rounding gives a simpler number that is still close enough.

$8.46 \div 7 = 1.2085714285714...$
 To 2 decimal places that is 1.21
 Close enough for almost any purpose

The one rule

- Find the digit in the rounding position.
- Look at the digit **immediately to its right**.
- 5 or more → round the digit up by 1.
- Less than 5 → leave the digit as it is.
- Then drop everything after it.

4.27 to 1 d.p. → look at 7 → round up → 4.3
 8.53 to 1 d.p. → look at 3 → leave it → 8.5

Decimal places

- Decimal places are counted **after** the decimal point.
- 1 d.p. means one digit after the point; 2 d.p. means two.
- Keep the zeros you need: 6.895 to 2 d.p. is 6.90, not 6.9, if the accuracy is being stated.

3.146 to 2 d.p. $\rightarrow$ 3.15
0.0752 to 2 d.p. $\rightarrow$ 0.08
14.203 to 2 d.p. $\rightarrow$ 14.20

When rounding up carries

- Rounding a 9 up makes it 10, so the carry moves along.
- Sometimes every digit changes.
- Do not panic — just add 1 in the rounding position and carry.

9.999 to 2 d.p. $\rightarrow$ 10
19.99 to 1 d.p. $\rightarrow$ 20
99.7 to the nearest whole number $\rightarrow$ 100

Rounding a division

- Work the division out to **one more place** than you need.
- Then round that answer.
- Work to one extra place, then round. Never round twice.

$8.46 \div 7$ to 2 d.p.
Work to 3 d.p.: 1.208...
Round: 1.21

Two warnings

- Round **once**, from the original number. Rounding in stages can push an answer the wrong way.
- A rounded answer is an approximation — say so, using “ $\approx$ ” or “to 2 d.p.”.

$2.4499 \rightarrow$ 1 d.p. directly $\rightarrow$ 2.4 ✓
 $2.4499 \rightarrow 2.45 \rightarrow 2.5$ x wrong
 $8.46 \div 7 \approx 1.21$ (2 d.p.)