

Name _____

Date _____

Unit 1 · Integers — revision sheet

Everything you need from every section. Read it before the end-of-unit test.

1.1 Adding and subtracting integers

- Integers are the positive and negative whole numbers together with zero: ... -3 , -2 , -1 , 0 , 1 , 2 , 3 ...
- Adding a positive number moves you **right** on the number line; subtracting a positive number moves you **left**.
- Adding a negative is the same as subtracting: $a + (-b) = a - b$.
- Subtracting a negative is the same as adding: $a - (-b) = a + b$.
- The further left a number is on the number line, the smaller it is, so $-7 < -3 < 0 < 2$.

Key words: integer · negative number · inverse · inverse operation · sum · difference

Integers: -200 , -7 , 0 , 1 , 43

Not integers: 0.5 , $-2\frac{1}{4}$, $\sqrt{10}$

-5 -4 -3 -2 -1 0 1 2 3 4 5

$-9 < -2 < 0 < 6$

$-8 + 5 = -3$ (start at -8 , move 5 right)

$6 + (-9) = 6 - 9 = -3$

$-7 - 4 = -11$

1.2 Multiplying and dividing integers

- positive × positive = positive** e.g. $6 \times 7 = 42$
- positive × negative = negative** e.g. $9 \times (-4) = -36$
- negative × negative = positive** e.g. $(-8) \times (-5) = 40$
- The same three rules apply to division.
- In a chain of multiplications, count the negative factors: an **even** number of negatives gives a positive answer, an **odd** number gives a negative answer.
- Watch the brackets: $(-4)^2 = 16$ but $-4^2 = -16$.

Key words: product · factor · quotient · index · inverse operation

$5 \times (-2) = (-2) + (-2) + (-2) + (-2) + (-2) = -10$

$(-8) \times (-5) = 40$

$9 \times (-4) = -36$

$-48 \div 6 = -8$

$-72 \div (-9) = 8$

$56 \div (-7) = -8$

$-3 \times (-4) \times (-2) = -24$ (3 negatives → negative)

1.3 Lowest common multiples

- The **multiples** of a number are its times table: multiples of 4 are 4, 8, 12, 16, 20, ...
- A **common multiple** of two numbers appears in both times tables.
- The **lowest common multiple (LCM)** is the smallest of those common multiples.
- Method: list the multiples of the **larger** number and stop at the first one that the smaller number divides into.
- If two numbers share no factors, $\text{LCM} = a \times b$, e.g. $\text{LCM}(5, 8) = 40$.
- If one number is a multiple of the other, the LCM is the larger number, e.g. $\text{LCM}(4, 12) = 12$.

Key words: multiple · common multiple · lowest common multiple (LCM) · digit

Multiples of 4: 4, 8, 12, 16, 20, 24, 28, ...
 Multiples of 6: 6, 12, 18, 24, 30, 36, ...
 Multiples of 4: 4, 8, 12, 16, 20, 24, 28, 32, 36 ...
 Multiples of 6: 6, 12, 18, 24, 30, 36 ...
 Common multiples of 4 and 6: 12, 24, 36, ...
 $\text{LCM}(4, 6) = 12$
 $\text{LCM}(9, 12) = 36$

1.4 Highest common factors

- A **factor** divides exactly into a number: the factors of 12 are 1, 2, 3, 4, 6, 12.
- A **common factor** divides into both numbers.
- The **highest common factor (HCF)** is the biggest of them.
- Method: list the factors of the **smaller** number, then work downwards and stop at the first one that also divides the larger number.
- If one number is a factor of the other, the HCF is the smaller number, e.g. $\text{HCF}(6, 18) = 6$.
- Useful fact: $\text{HCF} \times \text{LCM} = a \times b$, e.g. for 8 and 12: $4 \times 24 = 96 = 8 \times 12$.
- Dividing a fraction's numerator and denominator by their HCF simplifies it in one step.

Key words: factor · common factor · highest common factor (HCF) · co-prime · simplify

Factors of 24: 1×24 , 2×12 , 3×8 , $4 \times 6 \rightarrow 1, 2, 3, 4, 6, 8, 12, 24$
 Factors of 12: 1, 2, 3, 4, 6, 12
 Factors of 18: 1, 2, 3, 6, 9, 18
 Common factors: 1, 2, 3, 6
 $\text{HCF}(12, 18) = 6$
 $\text{HCF}(24, 36) = 12$
 $\text{HCF}(9, 20) = 1$

1.5 Tests for divisibility

- $\div 2$ — the last digit is even
- $\div 3$ — the sum of the digits is divisible by 3
- $\div 4$ — the number formed by the last two digits is divisible by 4
- $\div 5$ — the last digit is 0 or 5
- $\div 6$ — it passes the tests for both 2 and 3
- $\div 8$ — the number formed by the last three digits is divisible by 8
- $\div 9$ — the sum of the digits is divisible by 9
- $\div 10$ — the last digit is 0
- $\div 11$ — the difference between the sum of the odd-position digits and the sum of the even-position digits is 0 or a multiple of 11
- You can combine tests when the two divisors share no factors: a number divisible by 3 and by 4 is divisible by 12. But 2 and 4 *do* share a factor, so passing both does not guarantee divisibility by 8.

Key words: *divisible · tests of divisibility · remainder · digit sum · consecutive*

$15 \div 5 = 3$, so 15 is divisible by 5
 $15 \div 4 = 3$ remainder 3, so 15 is not divisible by 4
 4 530 $\rightarrow$ last digit 0 $\rightarrow$ divisible by 2, 5 and 10
 2 915 $\rightarrow$ last digit 5 $\rightarrow$ divisible by 5, not by 2 or 10
 $342 \rightarrow 3 + 4 + 2 = 9 \rightarrow$ divisible by 3 and by 9
 $8\ 514 \rightarrow 8 + 5 + 1 + 4 = 18 \rightarrow$ divisible by 3 and by 9
 $2\ 461 \rightarrow 2 + 4 + 6 + 1 = 13 \rightarrow$ divisible by neither

1.6 Square roots and cube roots

- Square numbers: 1, 4, 9, 16, 25, 36, 49, 64, 81, 100, 121, 144, 169, 196, 225, ...
- Cube numbers: 1, 8, 27, 64, 125, 216, 343, 512, 729, 1000, ...
- $\sqrt{\quad}$ undoes squaring, and $\sqrt[3]{\quad}$ undoes cubing — they are inverse operations.
- $\sqrt{144} = 12$ because $12^2 = 144$; $\sqrt[3]{125} = 5$ because $5^3 = 125$.
- To estimate $\sqrt{n}$ when n is not a square number, find the square numbers either side of it: $49 < 50 < 64$, so $7 < \sqrt{50} < 8$.
- 64 is special — it is both a square number (8^2) and a cube number (4^3).

Key words: *square number · square root · cube number · cube root · index · estimate*

1, 4, 9, 16, 25, 36, 49, 64, 81, 100, 121, 144, 169, 196, 225
 $12^2 = 144$
 $\sqrt{81} = 9$
 $\sqrt{400} = 20$
 $\sqrt{121} = 11$
 1, 8, 27, 64, 125, 216, 343, 512, 729, 1000
 $4^3 = 64$